

# Electromagnetic Energy Conversion ELEC0431

# Exercise session 2: Balanced three-phase systems

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### Laboratories – General information

- There are **four laboratories** to help you understand the theoretical and practical concepts:
  - > Transformers (mono-phase and three-phase)
  - > Synchronous machines
  - > Asynchronous machines
  - ➢ DC machines
- Each laboratory lasts at most 4 hours. They take place in the "pyramid" (building in front of the cafeteria of Montéfiore).
- You will be guided by student monitors and manuals during the laboratories. The manuals (one per laboratory) will soon be available on the webpage.
- It is strongly advised to get prepared before a laboratory by checking the corresponding manual.
- No report is asked. However, you will have to answer individually a quick evaluation at the end of each laboratory.
- The evaluation focuses exclusively on the concepts seen during the laboratory. You can be asked to:
  - $\succ$  Explain how a particular measurement was performed during the laboratory,
  - > Draw an equivalent circuit and use it for calculations,
  - Draw phasor diagrams,
  - $\succ$  Solve a problem encountered during the laboratory,
  - $\succ$  Etc.
- Each test represents 3.75 % of your final grade. That is 15 % of the grade for the four laboratories.
- Laboratories are mandatory (In case of unexcused absence, an absence grade will be given for the entire course).

### Laboratories – Schedule and groups

To create the laboratory schedule, you are required to fulfil the doodle "<u>https://cally.com/pmxdpjysb4mnkmzv</u>":

- By group of <u>4 students</u>, select <u>AT LEAST 6</u> available time slots (you may be given random sessions if less than 6 time slots were selected).
- In the space provided for names, write the STUDENT ID NUMBERS of all <u>4 MEMBERS</u> of the group (for example: "s161514, s171856, s164442, s179088").
- In the space provided for emails, write the email of <u>ONE reference student</u> in the group (which will be contacted in case of issues with the schedule).
- A time slot can be selected by maximum six groups, <u>do not delay in completing this Doodle</u>.
- In addition to your selected time slots, your schedule could include a laboratory session on the 19/04, 26/04, 10/05 and 17/05 mornings (Friday mornings in place of the traditional classes).

**IF AND ONLY IF** it is impossible for you to create a group of four students meeting the requirements, send me an email (florent.purnode@uliege.be).

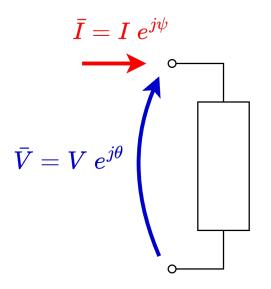
Make sure to complete the doodle by <u>23:59 on Friday, February 23<sup>rd</sup></u>, (Students who would not have given their availabilities by this time will be given random time slots).

- > Producer or consumer?
- ≻ Exercise 3 (homework 11)
- > Introduction to three-phase systems
- > Phase and line current/voltages Star and delta configurations
- $\succ$  Exercises 4 & 5

Using the <u>passive convention</u>, we consider a one-port crossed by a current  $\overline{I} = I e^{j\psi}$  with a voltage  $\overline{V} = V e^{j\theta}$ .

The associated complex power is

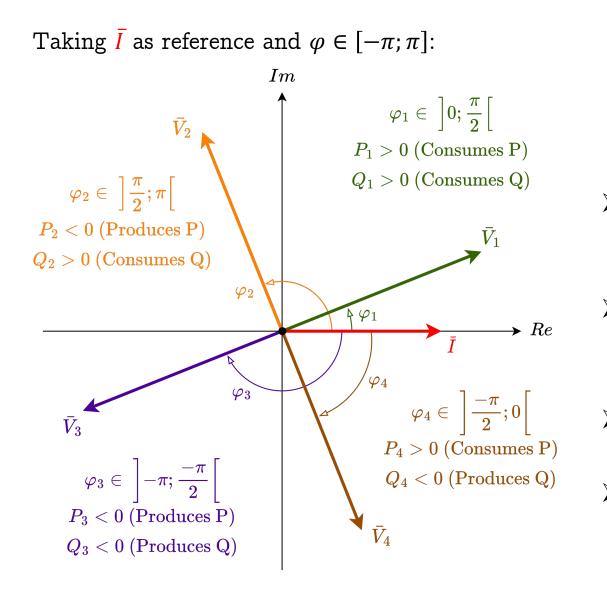
$$S = \overline{V} \,\overline{I}^* = VI \, e^{j(\theta - \psi)}$$
  
=  $VI \cos(\theta - \psi) + j \, VI \sin(\theta - \psi)$   
=  $P + j \, Q$ 



In case P is **positive**, we say that the one-port **consumes** active power. In case P is **negative**, we say that the one-port **produces** active power.

In case Q is **positive**, we say that the one-port **consumes** reactive power. In case Q is **negative**, we say that the one-port **produces** reactive power.

#### Producer or consumer ?



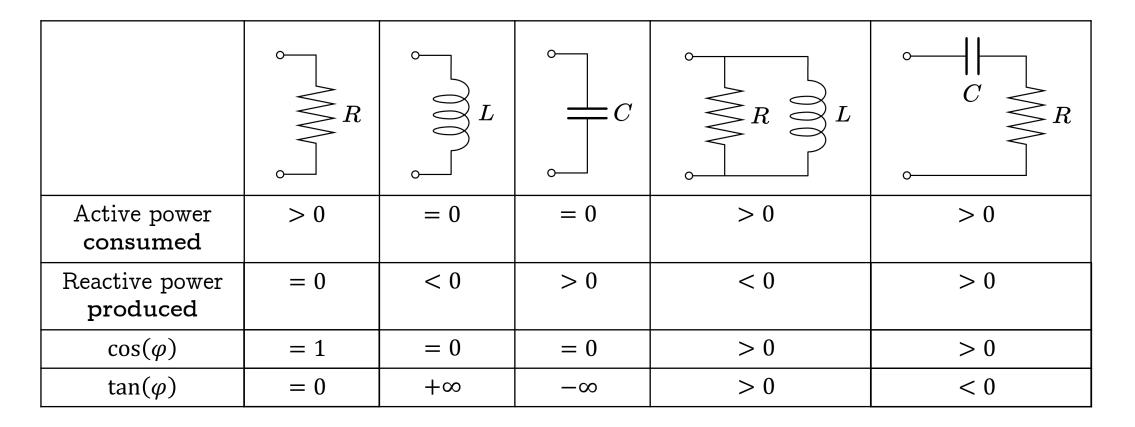
 $P = VI \cos(\theta - \psi) = VI \cos(\varphi)$  $Q = VI \sin(\theta - \psi) = VI \sin(\varphi)$ 

➢ If |φ| < π/2 The one-port consumes active power</li>
➢ If |φ| > π/2 The one-port produces active power

# Exercise 3 (Homework 11)

Fill the cells of the table below with the most appropriate answer among

 $= 0 < 0 > 0 = 1 < 1 + \infty - \infty$ 

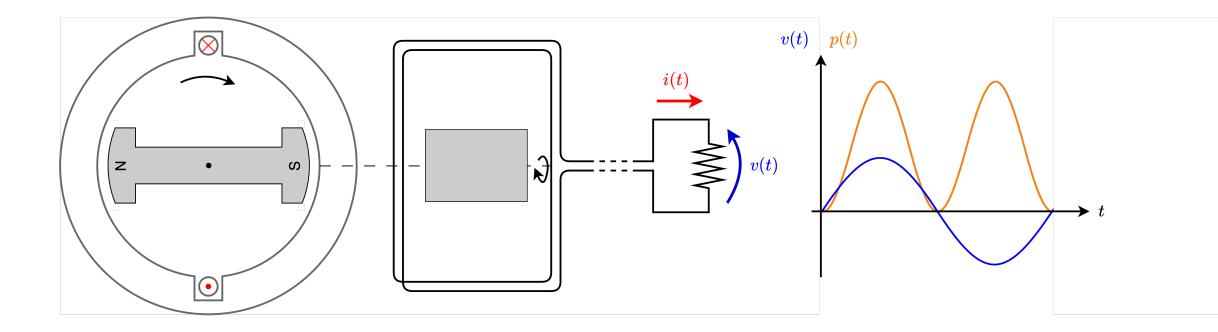


# Introduction to three-phase systems

One-phase generator Two-phase generator Three-phase generator Phase and line current/voltages – Star and delta configurations Exercises 4 & 5

#### One-phase generator

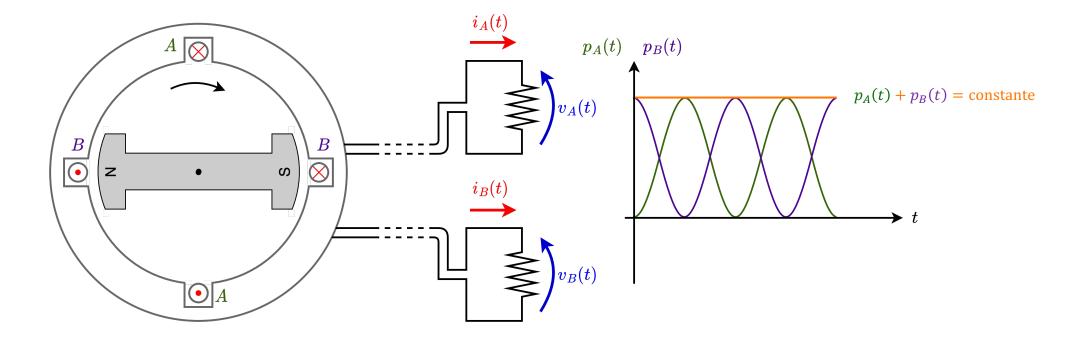
To build an AC generator, one could spin a magnet in a coil. A voltage v(t) is induced in the winding as it perceives a magnetic flux varying over time (Lenz).



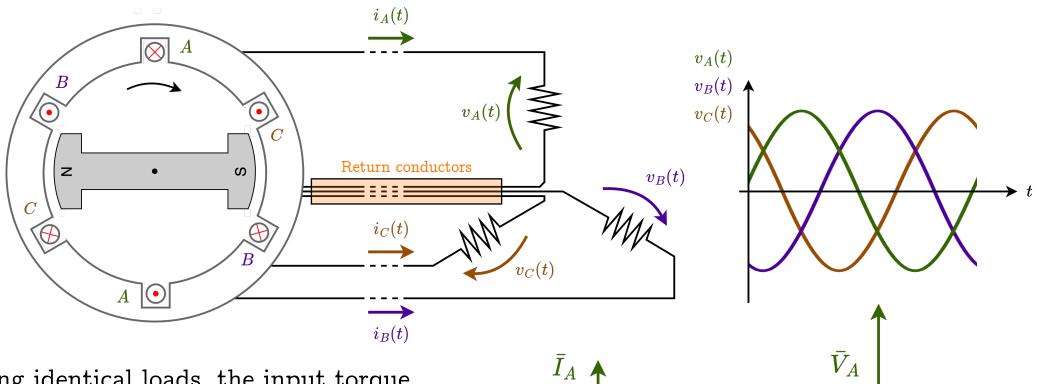
The output power p(t) fluctuates so that the input torque fluctuates as well. However, we would like to have a constant input torque.

#### Two-phase generator

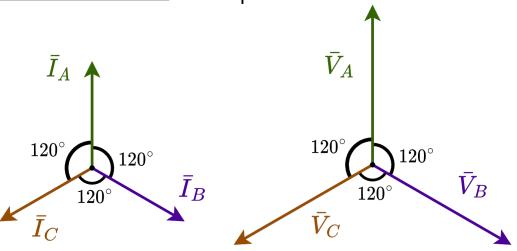
Using a second winding connected to <u>identical</u> loads, a constant input torque can be obtained.



### Three-phase generator

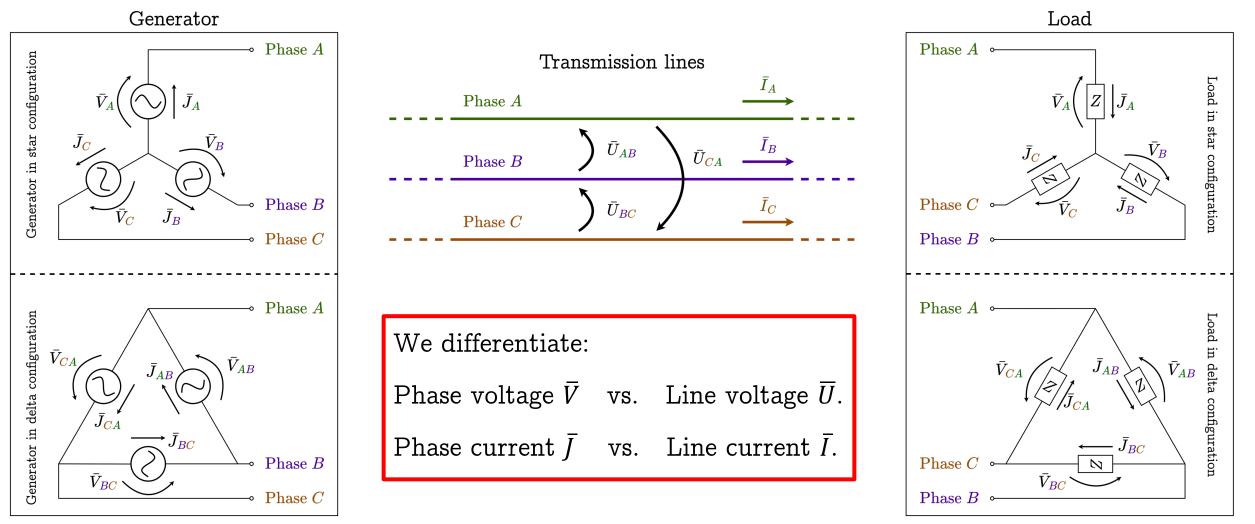


Using identical loads, the input torque also remains constant when using three phases. Moreover, plotting the current phase diagram, it appears that the sum of the currents is zero. The return conductors can thus be removed.



#### Three-phase circuits

Generators and loads are connected in star (\* or Y) or delta ( $\Delta$ ) configuration.



Some definitions:

The line voltage U is the voltage between any two transmission lines.

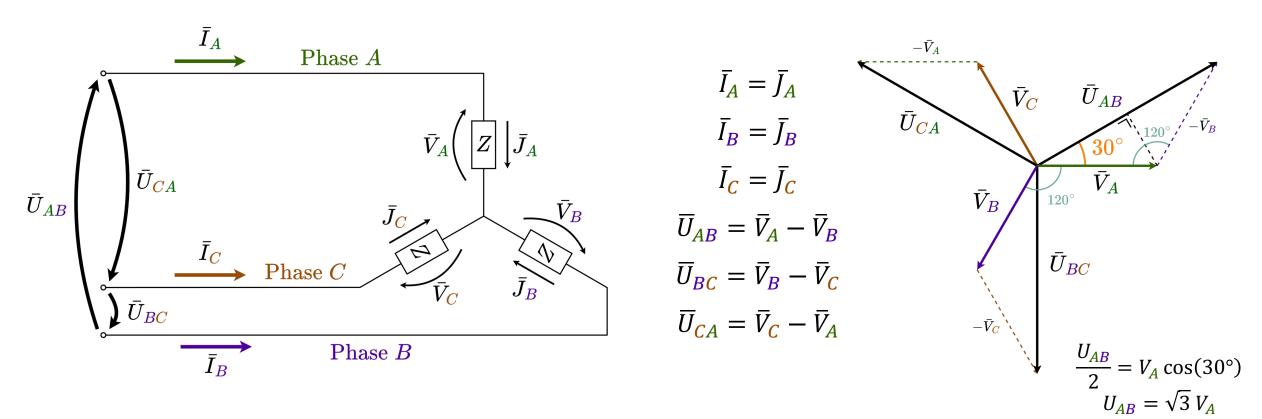
The line current I is the current flowing in a transmission line.

VS.

The phase voltage V is the voltage across any of the generator leg and/or load leg.

The phase current J is the current flowing in a generator leg and/or load leg.

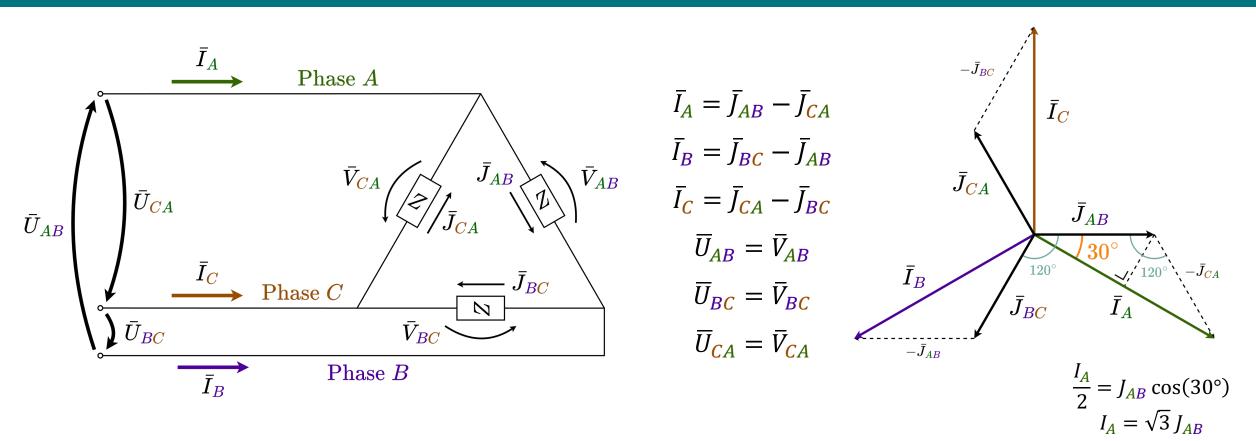
# Phase vs. line voltage/current – star configuration



In an equilibrated three-phase system in <u>star</u> configuration:

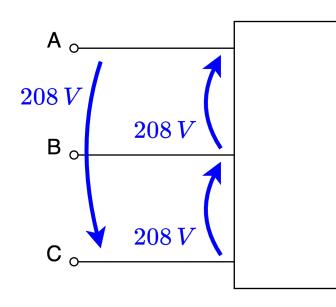
The norms of the phase and line currents are equal  $\Rightarrow I = J$ The norm of a line voltage is  $\sqrt{3}$  times the norm of a phase voltage  $\Rightarrow U = \sqrt{3} V$ 

# Phase vs. line voltage/current – delta configuration



In an equilibrated three-phase system in <u>delta</u> configuration:

The norms of the phase and line voltages are equal  $\rightarrow U = V$ The norm of a line current is  $\sqrt{3}$  times the norm of a phase current  $\rightarrow I = \sqrt{3}J$  Consider an electrical heater that dissipates 15 kW of power when connected to a three-phase power system of 208 V. As a first approximation, the heater is modelled as a purely resistive three-phase load.

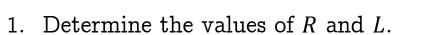


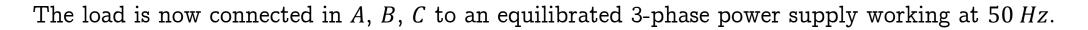
- 1. If no additional information is provided about the voltage, does the 208 V correspond to the peak or to the RMS value ?
- Compute the line current if the resistive loads are connected in \*.
- 3. If the resistors ae connected in  $\star$ , compute the resistance of each.
- 4. Compute the line current if the resistive loads are connected in  $\Delta$ .
- 5. If the resistors ae connected in  $\Delta$ , compute the resistance of each.

#### Exercise 5

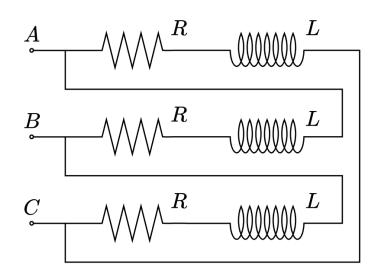
Consider the equilibrated 3-phase load showed on the right. To determine the value of the resistances and the value of the inductances, two tests are performed:

- A DC voltage of 150 V is applied between terminals A and B for a measured current of 1.95 A.
- An AC voltage of RMS value 230 V, oscillating at 50 Hz, is applied between terminals A and B for a measured RMS current of 2.81 A.





- 2. What is the phase shift  $\varphi$  between phase currents and corresponding phase voltages?
- 3. Draw on a phasor diagram the phase voltages, the phase currents, the line voltages and the line currents.



A load is connected to a 50 Hz single-phase generator of 20 V for an active power of 10 W with  $\cos \varphi = \frac{\sqrt{2}}{2}$ .

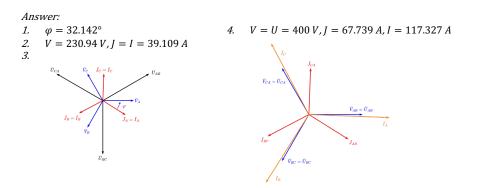
- 1. What is the reactive power Q?
- 2. Assuming the load is composed of a resistor and of an inductor in parallel, what are their values R and L?
- 3. The frequency is increased to 100 Hz. What is now the active and reactive powers consumed by the load?
- 4. A capacitor is placed in parallel of the load. Considering a frequency of 50 Hz, for which value C does the reactive power is 0?
- 5. In case the capacitor is placed in series of the load, derive the expression of the total equivalent impedance. In this configuration, derive the expression of the value of C for which the total reactive power is zero?

A load is composed of an inductor L = 10 mH in series with a resistor  $R = 5 \Omega$ .

1. Assuming a frequency of 50 Hz, what is the phase shift  $\varphi$ ?

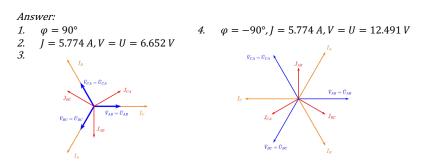
Three of these loads (identical) are set in a star configuration and connected to an equilibrated three-phase power supply working at 50 Hz. The amplitude of the line voltage U is 400 V.

- 2. What is the amplitude of the phase voltage V, of the line current I and of the phase current J?
- 3. Taking one phase voltage as reference, draw on a phasor diagram the phase voltages, the phase currents, the line voltages and the line currents.
- 4. Repeat point 2. and 3. in case the load is now connected in delta configuration.



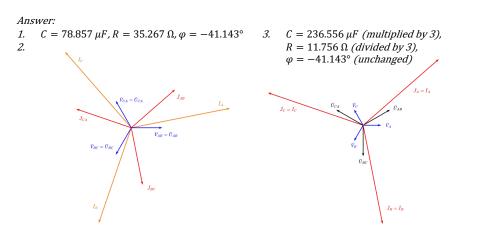
A three-phase load in delta configuration is connected to an equilibrated three-phase power supply working at 50 Hz. Each branch of the load is composed of an inductor (L = 10 mH) in series with a capacitor.

- 1. What is the phase shift  $\varphi$  in case C = 1.6 mF?
- 2. The amplitude of the line current is 10 A. Compute the amplitudes of the phase current J, of the line voltage U and of the phase voltage V.
- 3. Taking one phase voltage as reference, draw on a phasor diagram the phase voltages, the phase currents, the line voltages and the line currents.
- 4. Repeat point 1., 2. and 3. in case  $C = 600 \ \mu F$ .

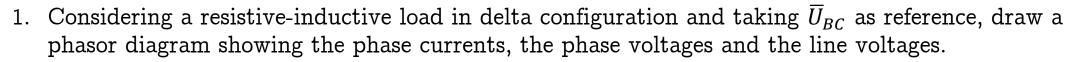


A three-phase load is connected to an equilibrated three-phase power supply working at 50 Hz. Each branch of the load is composed of a resistor in parallel with a capacitor.

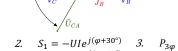
- 1. In case the load is connected in a delta configuration, a total three-phase active power  $P_{3-\varphi}$  of 4.5 kW is measured for an RMS line voltage of 230 V and an RMS line current of 15 A. Find the values of C, R and  $\varphi$ .
- 2. Taking one phase voltage as reference, draw on a phasor diagram the phase voltages, the phase currents, the line voltages and the line currents.
- 3. Repeat point 1. and 2. in case the load is connected in a star configuration. How does this modification impact the values of C, R and  $\varphi$ ?



Two wattmeters can be used to compute the active and reactive powers of an equilibrated three-phase system. The first wattmeter measures the current flowing in the first line  $\bar{I}_A$  and the voltage from the first to the second line  $\bar{U}_{BA} = -\bar{U}_{AB}$ . The second wattmeter measures the current flowing in the third line  $\bar{I}_C$  and the voltage from the third to the second line  $\bar{U}_{BC}$ .



- 2. Express the complex powers measured by the two wattmeters.
- 3. Show that one can compute the total three-phase active power as the opposite of the sum of the active powers measured by the two wattmeters  $(P_{3\varphi} = -P_1 P_2)$ .
- 4. Show that one can compute the total three-phase reactive power as  $\sqrt{3}$  times the difference of the active powers measured by the two wattmeters  $(Q_{3\varphi} = \sqrt{3}(P_1 P_2))$ .



Answer:

 $\bar{U}_{BC}$ 

wattmeter <sup>-</sup>

wattmeter 2

 $\bar{U}_{AB}$ 

 $\bar{I}_B$ 

 $\bar{U}_{B\ell}$ 

 $\bar{I}_C$